

ESS415/515 Midterm
Open Book, Open Note, Due at 12:20pm today 2/12/04

Question 1. Guiding Center Motion Effects on initial Maxwellian Distributions

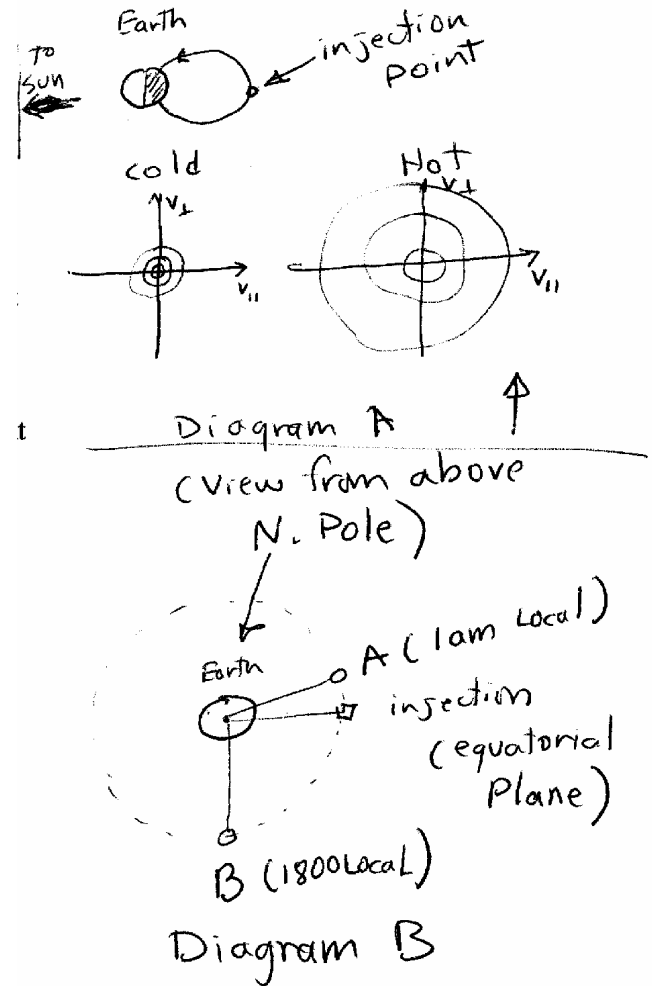
Given: Two isotropic particle distributions, with low and high energy particle populations, are continuously injected on the magnetic equator at 3Re geocentric distance from the Earth at the longitude of midnight (see Diagram A).

The low energy distribution has a temperature equivalent energy of 1eV and the high energy distribution has a temperature equivalent energy of 10 keV. Assume there are no other significant sources of particles in the magnetosphere and ignore electrons except as a background which keeps the overall plasma quasi-neutral.

1. **Describe** the total ion distribution function at the equator, at 3Re, as a function of time at Point A, which is 15 degrees east of midnight (see Diagram B)

2. **Describe** the total ion distribution function at the equator, at 3Re, as a function of time, at Point B, which is 90 degrees West of midnight (see Diagram B).

HINT: Consider times from minutes to days, and all appropriate guiding center drifts which might be applicable in a static magnetosphere.



Question 2: Compare **Curvature and Gradient Drift** rates for a 100 keV electron at L=6 which mirrors just above the ionosphere. Plot the ratio of curvature drift over

gradient drift: $\frac{W_{\text{Curv}}}{W_{\nabla B}}$ along the field line

Problem 3. Adiabatic Invariants

a) **Give** expressions for each of the three adiabatic invariants of charged particle motion in a static magnetic dipole field.

b) Assume there is a uniform, time-varying electric field E across the whole

magnetosphere in the dawn-to-dusk direction given by $E = E_0 \cos(2\pi t / \tau)$

where $\tau = 600$ seconds (or 10 minutes).

1) **How** will this E field affect each of the 3 adiabatic invariants of motion for typical magnetospheric particles?

2) For those particles resonant with this E -field at $L=6$, **What** is the maximum energy they could gain by radial diffusion caused by this E -field in the magnetosphere?